The mid- and far-infrared colours of AGB and post-AGB stars

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ABSTRACT

With the advent of space missions, like SPITZER and ASTRO-F, with sensitive detectors in the near- and mid-infrared covering a reasonable field-of-view and having a good spatial resolution, it will be possible to detect individual AGB stars in Local Group galaxies. The filters used by these missions are non-standard and different from mission to mission. In this paper, the colours of mass-losing AGB and post-AGB stars are calculated in the broad-band filters of the SPITZER and ASTRO-F missions, as well as Bessell V, I and 2MASS J, H, K to connect these results to existing ground-based data. The models are calculated for carbon- and oxygen-rich chemistry and cover different effective temperatures and dust compositions.

Key words. circumstellar matter – stars: mass loss – stars: AGB and post-AGB

1. Introduction

Asymptotic Giant Branch (AGB) and post-AGB stars are prominent emitters in the infrared (IR), firstly because of their low effective temperatures and secondly because of their mass loss rates, which can go up to $10^{-4} M_\odot$ yr$^{-1}$ for brief spells of time, in conjunction with dust formation. The importance of the mid-IR was first demonstrated by the results of the IRAS mission (Beichman et al. 1988) which discovered many mass-losing AGB stars (e.g. van de Veen & Habing 1988) in the solar neighbourhood but also luminous mass-losing AGB stars in the Large Magellanic Cloud (LMC) (see Reid et al. 1990; Reid 1991; Wood et al. 1992; Zijlstra et al. 1996; Loup et al. 1997), and Small MC (Whiteock et al. 1989; Groenewegen & Blommaert 1998), at the limiting magnitudes of IRAS near 100 mJy at 12 micron. When the ISO satellite was launched many of these mass-losing AGB stars discovered by IRAS in the MCs were followed up (e.g. Trams et al. 1999; van Loon et al. 1999), and new surveys in the MCs were conducted (Loup et al. 1999a,b), in particular using the ISOCAM instrument (Cesarsky et al. 1996; Blommaert et al. 2003) that had imaging filters covering 3 to 15 micron with a field-of-view of typically 1.5$'$ by 1.5$'$. In addition, the Galactic Centre region, where IRAS was severely confusion limited, was imaged during the ISOGAL survey (Omont et al. 2003), discovering many AGB stars (Omont et al. 1999).

IRAS and ISO showed the importance of the IR region, from the Near-IR to the Far-IR. The SPITZER mission (Werner et al. 2004), launched on 25 August 2003, and the ASTRO-F mission (e.g. Pearson et al. 2004; Matsuhura et al. 2005), with a planned launch date of spring 2006, carry a range of imaging filters that cover the near-, mid- and far-IR. Due to an improved sensitivity and spatial resolution it is expected to resolve individual AGB stars in galaxies far beyond the MCs.

In the present work, series of dust radiative transfer models are presented that cover the spectral types, dust composition and mass loss rates seen for Galactic AGB stars. The flux-densities are computed in the SPITZER IRAC (Fazio et al. 2004) and MIPS (Rieke et al. 2004) filters, and the ASTRO-F IRC, MIR-S, MIR-L and FIS filters. For comparison to ground based data $V$, $I$ and $J$, $H$, $K$ magnitudes are also presented.

Section 2 presents the radiative transfer model and the inputs to it, including the various dust compositions considered. Section 3 gives details on the considered filter curves and the adopted flux-calibration. Section 4 presents the results, scaling laws to arbitrary luminosities and distances, and some caveats in the use of the results. Section 5 concludes by illustrating colour-magnitude diagrams for AGB stars in M 31 and the Wolf-Lundmark-Melotte (WLM) galaxy.

Earlier results from this kind of dust modelling (in particular for the ISOCAM filters) were available as private communication and have been used in Blommaert et al. (2000), Ortiz et al. (2002) and Ojha et al. (2003).

2. Inputs to the radiative transfer model

The models have been calculated with a 1-dimensional dust radiative transfer (RT) code that solves the radiative transfer equation and the thermal balance equation in a self-consistent way (Groenewegen 1993, also see Groenewegen 1995).
Fig. 1. The absorption efficiency for the five dust species considered here, plotted over the whole wavelength range (top panel), and the mid-IR. Dashed lines indicate 100% AMC, and the combination of 85% AMC +15% SiC, which peaks near 11.3 µm. The solid lines indicate 100% silicate (with a narrow feature that peaks near 10 µm), 40% silicate + 60% AlOx, and 100% AlOx (with a broad feature that peaks near 12 µm).

Basic inputs to the model are the stellar luminosity (L), distance (d), photospheric spectrum, (total) mass loss rate, dust-to-gas ratio, (terminal) outflow velocity, dust condensation temperature (T_c) and composition of the dust.

The models have been calculated for (arbitrary) values of L = 3000 L☉, d = 8.5 kpc, v∞ = 10 km s⁻¹, dust-to-gas (µ) ratio = 0.005, and no interstellar reddening. Scaling relations will be presented later.

Photospheric input spectrum for O-rich stars are taken from Fluks et al. (1994) for spectral types M0 (T_eff = 3850 K), M6 (T_eff = 3297 K) and M10 (T_eff = 2500 K). For C-rich stars the models by Loidl et al. (2001) for T_eff = 3600 and 2650 K are considered¹.

Several types of dust are considered that cover the main features observed in AGB stars. The absorption coefficients as a function of wavelength are displayed in Fig. 1. For dust around O-rich stars they are:

- 100% Aluminium Oxide (AlOx; amorphous porous Al₂O₃), with optical constants from Begemann et al. (1997) and assuming a condensation temperature of T_c = 1500 K.
- A combination of 60% AlOx and 40% Silicate (optical constants from David & Pegourie 1995) and assuming a condensation temperature of T_c = 1500 K.

The dust species with 60 to 100% AlOx can explain the observed Spectral Energy Distributions (SEDs) and ISOCAM CVF 5-14 µm spectra in Galactic Bulge AGB stars which have mass loss rates up to 10⁻⁷ M☉ yr⁻¹ (Blommaert 2003; Blommaert et al. 2005, in preparation).

- 100% silicate with T_c = 1000 K.

For dust around C-rich stars two species are considered:

- A combination of 85% Amorphous Carbon (AMC) and 15% Silicon Carbide (SiC) with optical constants from, respectively, Rouleau & Martin (1991) for the AC1 species and α-SiC from Pégourié (1988). A T_c of 1200 K is adopted.
- 100% AMC with a T_c of 1000 K.

This range of AMC with zero to 15% percent SiC and the corresponding condensation temperatures can explain the SEDs and IRAS LRS spectra of the majority of (Galactic) C-stars (Groenewegen 1995; Groenewegen et al. 1998). For all dust species a uniform grain size of 0.1 µm is adopted.

### 3. Flux calibration

In this paper the broad-band filters of the SPITZER and ASTRO-F missions are considered. Both contain filters in the near- and mid-IR which are ideal to identify mass losing stars. Filter curves have been obtained from official websites², and are reproduced in Fig. 2. The filter names and their central wavelengths are given in Table 1.

To connect this data to existing ground-based data Bessell V, I and 2MASS J, H, K magnitudes are also calculated, whose filter curves are also shown in Fig. 2.

The main output of the RT code is the flux emerging from the AGB star and its dust envelope. This flux is folded with the filter curves and flux-densities and magnitudes are calculated from (following the definition used by IRAS, ISOCAM and IRAC, see e.g. Blommaert et al. 2003):

$$m_λ = -2.5 \log \left( \frac{\int (λ/λ_0) F_0 R_λ dλ}{\int R_λ dλ} \right) + m_0.$$  \hspace{1cm} (1)

The zero-points, m_0, are calculated from a reference spectrum for Vega calculated using the MARCS code (Decin, private communication). The resulting and adopted flux-densities for a zero-magnitude star are listed in Table 1.

¹ And with a C/O ratio of 1.1.

Table 1. Adopted flux-densities for a zero-magnitude star.

<table>
<thead>
<tr>
<th>Filter</th>
<th>( \lambda_0 ) (( \mu )m)</th>
<th>Flux (Jy)</th>
</tr>
</thead>
<tbody>
<tr>
<td>IRAC_3.6</td>
<td>3.55</td>
<td>278.8</td>
</tr>
<tr>
<td>IRAC_4.5</td>
<td>4.49</td>
<td>179.6</td>
</tr>
<tr>
<td>IRAC_5.8</td>
<td>5.73</td>
<td>118.4</td>
</tr>
<tr>
<td>IRAC_8.0</td>
<td>7.87</td>
<td>63.5</td>
</tr>
<tr>
<td>MIPS_24</td>
<td>24</td>
<td>7.23</td>
</tr>
<tr>
<td>MIPS_70</td>
<td>70</td>
<td>0.791</td>
</tr>
<tr>
<td>MIPS_160</td>
<td>160</td>
<td>0.190</td>
</tr>
<tr>
<td>IRC_N2</td>
<td>2.69</td>
<td>651.4</td>
</tr>
<tr>
<td>IRC_N3</td>
<td>3.06</td>
<td>323.5</td>
</tr>
<tr>
<td>IRC_N4</td>
<td>4.55</td>
<td>199.8</td>
</tr>
<tr>
<td>MIRS_S7</td>
<td>8.0</td>
<td>84.5</td>
</tr>
<tr>
<td>MIRS_S9W</td>
<td>10.04</td>
<td>57.7</td>
</tr>
<tr>
<td>MIRS_S11</td>
<td>10.0</td>
<td>32.0</td>
</tr>
<tr>
<td>MIRI_L15</td>
<td>17.5</td>
<td>17.6</td>
</tr>
<tr>
<td>MIRI_L18W</td>
<td>17.6</td>
<td>11.0</td>
</tr>
<tr>
<td>MIRI_L24</td>
<td>23.55</td>
<td>7.45</td>
</tr>
<tr>
<td>FIS_N60</td>
<td>60</td>
<td>0.935</td>
</tr>
<tr>
<td>FIS_WIDE-S</td>
<td>90</td>
<td>0.604</td>
</tr>
<tr>
<td>FIS_WIDE-L</td>
<td>140</td>
<td>0.194</td>
</tr>
<tr>
<td>FIS_N160</td>
<td>160</td>
<td>0.166</td>
</tr>
</tbody>
</table>

4. Results for AGB and post-AGB stars

As mentioned before, the results of the numerical code have already been used to successfully fit the SEDs of individual stars (Groenewegen 1994a,b, 1995, 1997; Groenewegen et al. 1995, 1997, 1998) and predict the colours of AGB stars (Blommaert et al. 2000; Ortiz et al. 2002; Ojha et al. 2003) and has been bench-marked against other codes (Ivezic et al. 1997). To illustrate the typical accuracies that can be achieved in fitting SEDs and colours, Fig. 3 shows a fit to the SED and the IRAS LRS spectrum of the Mira V Oph (cf. Fig. 33 in Groenewegen et al. 1998), but now with the 2650 K model atmosphere instead of a black-body in Groenewegen et al. (1998). The agreement is quite good over the whole wavelength range.

Figure 4 shows colour-colour diagrams of \((J - K)\) versus \((J - H)\), \((J - [3.6])\) and \((J - [4.5])\) (the latter two being representative for \((J - L)\) and \((J - M)\), respectively). The data are the mean \(JHKLM\) magnitudes of carbon and oxygen-rich stars based on the monitoring of the light curves from Le Bertre (1992, 1993) and Taranova & Shenavrin (2004). Only stars with magnitudes in all bands and without uncertain magnitudes were considered.
Fig. 3. Model fit to the SED and IRAS LRS spectrum of the carbon Mira V Oph (cf. Groenewegen et al. 1998). Used is the 2650 K model atmosphere, \( L = 4390 L_\odot \), \( d = 0.68 \) kpc, \( \dot{M} = 3.0 \times 10^{-8} M_\odot \) yr\(^{-1}\), and a combination of 85% AMC and 15% SiC.

Although such a comparison between models and data is not trivial because of the effects of reddening (although most sources are within 2.5 kpc and reddening at these wavelengths should be small) and the fact that the IRAC [3.6] and [4.5] filters are not directly comparable to \( L \) and \( M \), it may nevertheless illustrate the overall correctness of the models, as suggested by the referee. Again, the overall agreement between models and data is quite good with most data points within 0.1 magnitude of any of the sequences.

The results of the models obtained in the present paper for the \( V, I, J, H, K \), IRAC, MIPS and ASTRO-F magnitudes and fluxes are listed in Tables A.1 to A.26 for AGB stars and Tables A.27 to A.36 for post-AGB stars. Table A.1 is repeated as Table 2 to illustrate the content.

The AGB models have been calculated for mass loss rates up to a value resulting in a \((J - K)\) colour of about 10, roughly the reddest known AGB stars (Groenewegen et al. 1998). For every set of input in terms of stellar input spectrum and dust composition there are two tables, listing, respectively, \( V, I, J, H, K \) (in magnitudes) and the flux-densities (in mJy) for SPITZER IRAC and MIPS, and the flux-densities (in mJy) for the ASTRO-F IRC, MIR-S, MIR-L and FIS filters. Tables A.1–A.26 also list the mass loss rate and the dust optical depth, at 11.75 \( \mu \)m for AMC+SiC and 11.33 \( \mu \)m for AMC, 11.75 \( \mu \)m for AlOx and AlOx+silicate, and 10.20 \( \mu \)m for silicate. Optical depths at other wavelengths can be estimated from Fig. 1. For the post-AGB models the dust temperature at the inner radius is listed instead of the mass loss rate. By decreasing this parameter the expansion of the dust envelope after cessation of mass loss at the end of the AGB can be simulated. The post-AGB tracks have only been calculated for the 100% sil-
cate and 100% AMC models, as it appears that dust with appreciable amounts of, respectively, AlOx and SiC only appear at lower mass loss rates, and not at the tip of the AGB. The model runs are such that the first entry for the post-AGB models corresponds to the same parameter set as for the last entry in the corresponding AGB model (e.g. Tables A.27–A.3, A.29–A.11, A.34–A.24) but listed as the result of an independent calculation. One can notice small differences of ≤1% in the fluxes and this is due to the accuracy of the RT model at these large optical depths.

### 4.1. Scaling laws

The fluxes listed in the tables scale with \((L/3000)/(d/8.5)^2\) (and the magnitudes as \(-2.5 \log\) of this factor).

The spectral energy distribution is for a given stellar input spectrum-determined only by the dust optical depth, defined by (Groenewegen 1993, 1995):

\[
\tau_d = \int_{a_{\text{min}}}^{a_{\text{max}}} \pi a^2 \kappa_d(a) \rho_d(a) \, da
\]

\[
= 5.405 \times 10^8 \frac{M \Psi Q_d/a}{R_\ast} v_{\text{to}} \rho_d(a) \int_{1}^{a_{\text{max}}} \frac{R(x)}{x^2} \, dx \tag{2}
\]

where \(n_d\) is the number density of dust particles, \(x = r/r_\ast\) and \(M(r) = M R(x)\). The units are: the (present-day) mass loss rate at the inner radius \(M\) in \(M_\odot\,\text{yr}^{-1}\), \(\Psi\) the dust-to-gas mass ratio, \(Q_d/a\) the absorption coefficient of the dust over the grain radius in \(\text{cm}^{-1}\), \(R_\ast\) the stellar radius in solar radii, \(v_{\text{to}}\) the terminal velocity of the circumstellar envelope in \(\text{km}\,\text{s}^{-1}\), \(\rho_d\) the dust grain density in \(\text{g}\,\text{cm}^{-3}\), \(r_\ast\) the inner dust radius in stellar radii and \(x_{\text{max}}\) the outer radius in units of \(r_\ast\). For the assumptions adopted in the present paper—a constant velocity and mass loss rate, and a outer radius much larger than the inner radius—the integral becomes unity.

This relation implies a necessary scaling when the expansion velocity and/or dust-to-gas ratio and/or luminosity are different from the nominal ones, and this scaling is like \(M \sim (v/10 \,\text{km}\,\text{s}^{-1}) \, (0.005/\Psi) \, \sqrt{L/3000}\).

### 4.2. Caveats

My expectation is that these tracks might be useful to identify AGB stars in colour–colour and colour–magnitude diagrams that will become available when SPITZER and ASTRO-F results on external galaxies become available. Such a comparison might also be useful to provide indications of the chemical type and dust optical depth. However, when doing such comparisons some limitations of the models must be kept in mind.

- AGB stars are variable, usually of the Semi-Regular or Mira type. Mira variables can have pulsation amplitudes corresponding to 6–8 magnitudes in \(V\), and up to 2.5 mag in \(K\). 1.5 mag in \(M\) and 1.3 mag in \(N\) (e.g. Le Bertre 1992, 1993, Groenewegen et al. 1998). Little is known about the level of variability in the mid-IR, but for example CW Leo (IRC +10 216), with a full-amplitude in \(K\) of 2.0 mag (Le Bertre 1992), still has a full-amplitude at 850 \(\mu\text{m}\) of 0.24 mag (Jenness et al. 2002).

- Other dust components may be present that are not taken into account (MgS near 35 \(\mu\text{m}\) in carbon stars, e.g. Hony et al. 2002, several crystalline silicate complexes near 23, 28, 33, 40 and 60 \(\mu\text{m}\), see e.g. Molster et al. 2002) and that may influence some fluxes, especially below ~60 \(\mu\text{m}\).

- The dust shell may be non-spherical and scattered light might play a role.

- The models have been calculated assuming a constant mass loss rate. This may affect the far-IR colours (beyond ~100 \(\mu\text{m}\)) either way.
The photospheric models used are appropriate for solar metallicities. This implies possible shifts in colour for low optical depths where the photosphere dominate the colours in systems of non-solar metallicity.

The post-AGB model have been calculated under the assumption that the effective temperature and luminosity do not change over the time for the dust shell to drift away. For example, in the case of the 2650 K effective temperature C-rich central star, with a luminosity of 3000 $L_\odot$ and 10 km s$^{-1}$ expansion velocity it takes about 1100 year for the dust shell to expand to an inner dust radius temperature of 100 K, 8300 yr to 50 K, and 600000 yr to 10 K. The transition timescale between the end of the AGB and the start of the PN phase (typically assumed to start at 10 000 K) is highly uncertain, and depends on the core mass (i.e. initial mass) of the star (the larger, the faster the evolution). Typical values are thought to be between 500 and 1500 years (e.g. Marigo et al. 2001, 2004).

This implies that only for inner dust radius temperatures above $\gtrsim$150 K the flow timescale is short enough for the assumption of constant luminosity and effective temperature likely to be valid.

The final calibration may differ from the adopted one once the total throughput of the system has been established in-orbit.

5. Discussion

Dust radiative transfer models for (post-)AGB stars are presented from the optical to the far-infrared. The models are calculated in view of the (upcoming) results from SPITZER and (hopefully) ASTRO-F. They may be useful to identify AGB stars, and provide rough estimates of spectral type, luminosity and mass loss rate. I warn again, though, that once candidate AGB stars have been selected, the best estimates for mass loss rate, luminosity and dust composition can only be obtained by detailed fitting of the entire SED (and spectra if available) of individual stars.

As an illustration, Figs. 5 and 6 show some tracks in a colour–magnitude diagram for, respectively, SPITZER IRAC filters for an AGB star of 3000 $L_\odot$ at a distance of 932 Kpc (appropriate for WLM, McConnachie et al. 2005), and SPITZER MIPS filters for an AGB star of 3000 $L_\odot$ at a distance of 785 Kpc (appropriate for M31, McConnachie et al. 2005). WLM and M31 are actual targets for those instruments according to the Spitzer Reserved Observations Catalog. One can observe that the tracks of the C- and O-rich mass-loss sequence largely overlap in [3.6–4.5] colour. Also the post-AGB tracks cover the same range in this colour. On the other hand, the [3.6] magnitude is a good indicator of the luminosity and the [3.6–4.5] colours of the mass loss rate. By comparison, in Fig. 6 C- and O-rich models separate, as well as AGB from post-AGB models. This illustrates the usefulness of a 70 $\mu$m filter to trace post-AGB evolution. The MIPS 24 $\mu$m filter traces the wing of the silicate 18 $\mu$m feature and therefore the 24 $\mu$m magnitude brightens quickly with the onset of mass-loss, so that the [24–70] colour initially becomes negative for O-rich stars. On the other hand, luminosity and mass loss rate are difficult to discriminate as the AGB sequence is almost vertical in [24–70] colour.

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